Fifth exercise sheet for the lecture

# XML and Programming Languages 

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## Exercise 15

Consider the CoreXPath query /descendant $:: a /$ preceding $:: b[$ ancestor $:: c]$.

1. Give an equivalent query without reverse axis steps.
2. What would be generally applicable rules for doing the above transformation?

## Exercise 16

Check query containment for each combination of the following CoreXPath expressions: $a / b / c, a / b[c] / *, a / b[*] / c, a / * / c$, and $* / b / c$.

## Exercise 17

Find a minimal, equivalent Simple CoreXPath expression for $r[(a[b] / c) \wedge d] / d$. What further simplification would be possible if we knew that all inputs satisfy the DTD $\left(r,\left\{r \rightarrow a^{*} d e, a \rightarrow(b|f| \epsilon) c, b \rightarrow c \mid \epsilon, c \rightarrow d, d \rightarrow \epsilon, e \rightarrow\right.\right.$ $\epsilon, f \rightarrow \epsilon\})$ ?

## Exercise 18

Consider the following formulas in first-order logic using only two variables:

1. $\phi(x)=\exists y$. descendant $(y, x) \wedge \neg \operatorname{child}(x, y) \wedge \operatorname{lab}_{a}(y)$
2. $\phi(x)=\exists y$. descendant $(y, x) \wedge \neg \operatorname{child}(y, x) \wedge \operatorname{lab}_{a}(y)$
3. $\phi(x)=\exists y$. $\neg$ following-sibling $(y, x) \wedge \operatorname{lab}_{a}(y)$
4. $\phi(x)=\exists y$. $\left(\exists x . \operatorname{child}(y, x) \wedge \operatorname{lab}_{a}(x) \wedge \operatorname{lab}_{b}(y)\right)$

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\wedge \operatorname{descendant}(y, x) \wedge \neg \operatorname{child}(y, x)
$$

For each, give an equivalent CoreXPath filter expression.

