

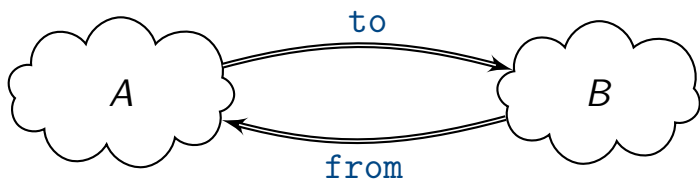
# **Bidirectional Transformations**

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## **a PL perspective**

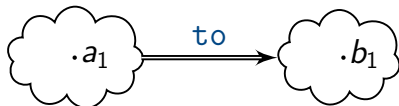
BIRS meeting on BX, 2013

## Bidirectional Transformations (BX)

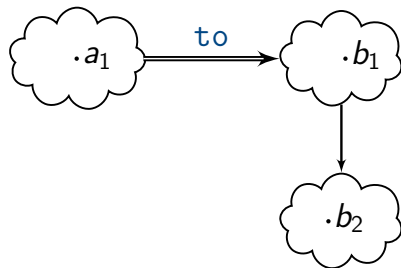


database source	$\Leftrightarrow$	materialized view
software model	$\Leftrightarrow$	code
document representation	$\Leftrightarrow$	screen visualization
concrete syntax	$\Leftrightarrow$	abstract syntax
abstract datatype	$\Leftrightarrow$	actual implementation
program input	$\Leftrightarrow$	program output

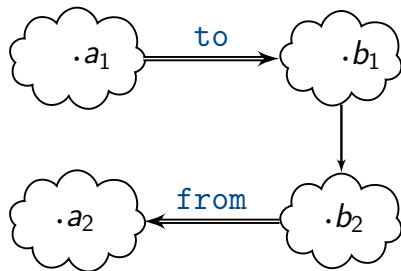
# Bidirectional Transformations



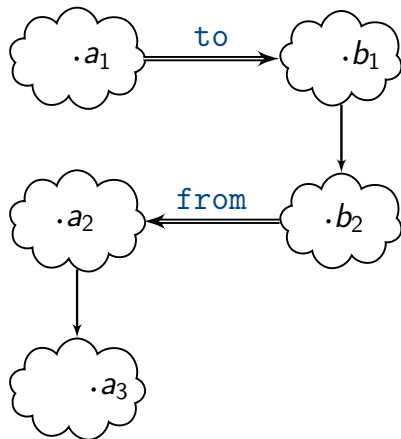
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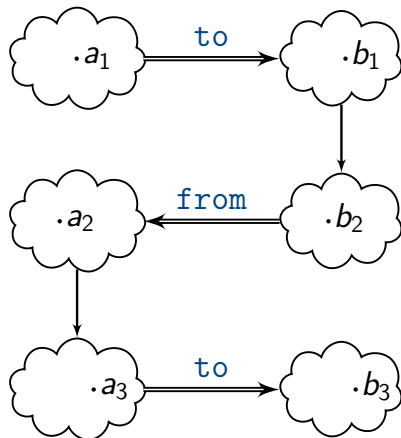
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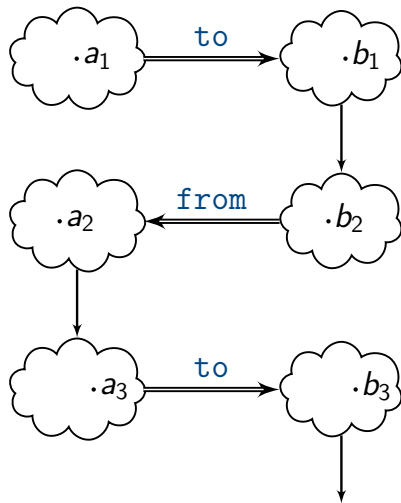
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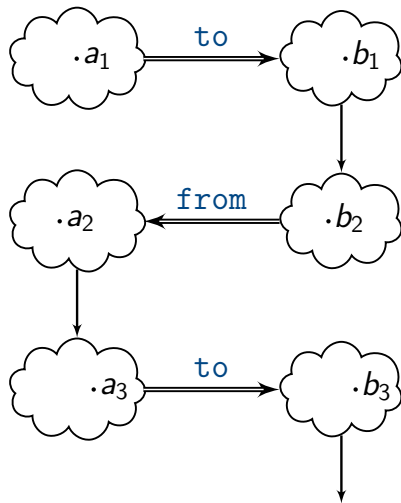


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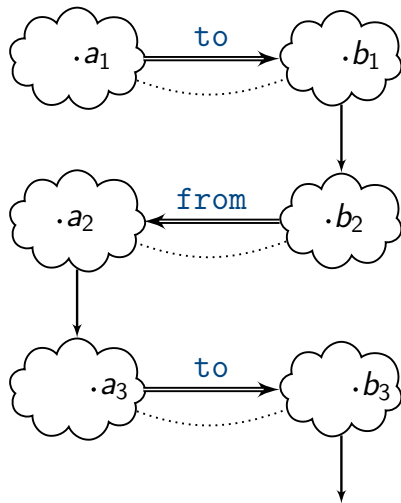


## Bidirectional Transformations



unless bijective, typically  
additional information  
needed/useful

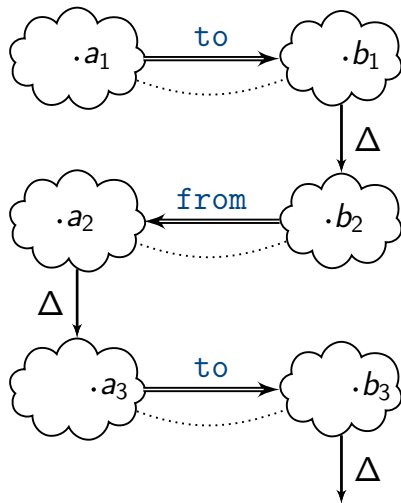
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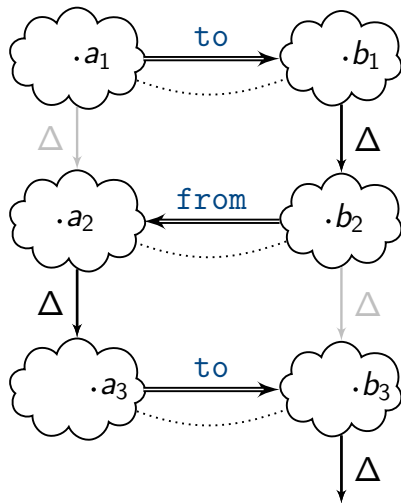
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## Objectives for this Talk

- ▶ get everybody into “BX mode” for the week
- ▶ set out basic premises of the PL approach, paradigmatic problems
- ▶ introduce terminology and semantic principles
- ▶ no details of specific solutions
- ▶ relate to what “we” think is solved and what not
- ▶ open discussion

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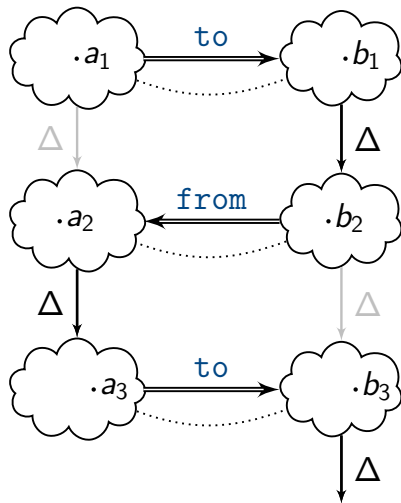
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- ▶ being driven by our favourite new PL techniques
- ▶ typically, algebraic data domains

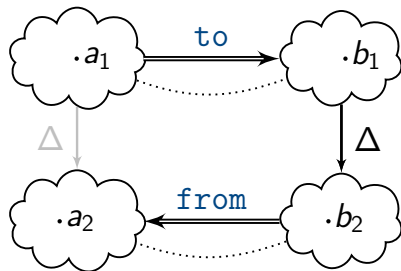
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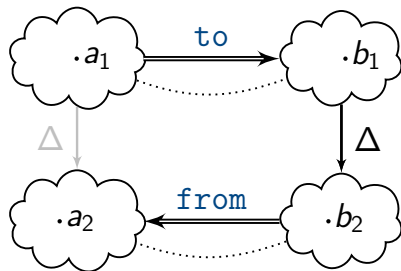
# Bidirectional Transformations



focus on:

- ▶ single-side updates
- ▶ one-step updates

## Bidirectional Transformations



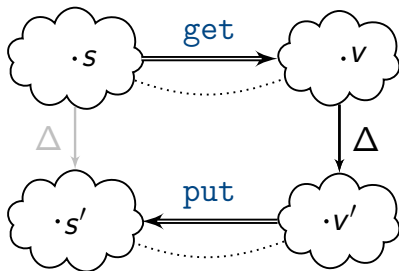
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also, focus on asymmetric setting:

- ▶ **to** usually non-injective, henceforth called **get**
- ▶ **from** then called **put**, definitely needs extra info
- ▶ for simplicity, state-based
- ▶ “sources” and “views”

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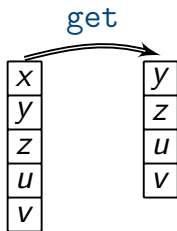
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## Bidirectional Transformations

A closer look at representing  $S \cdot V$  connections.

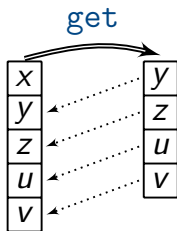
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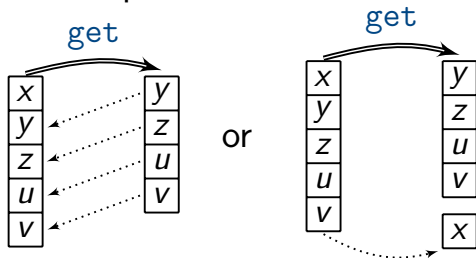
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## Bidirectional Transformations

A closer look at representing  $S \rightarrow V$  connections.

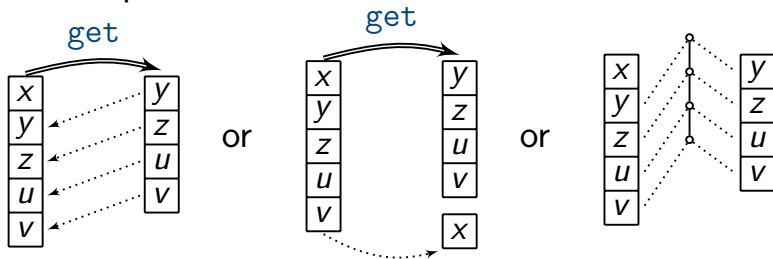
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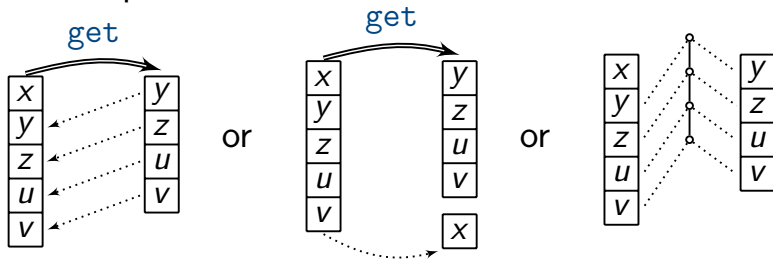
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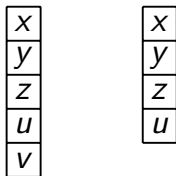
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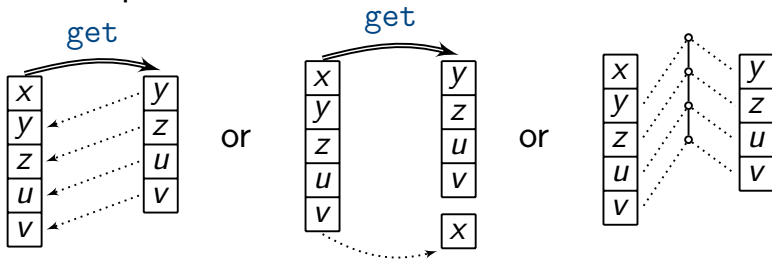
Why is it not enough to look just at the data?



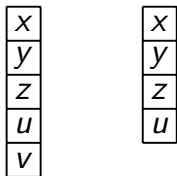
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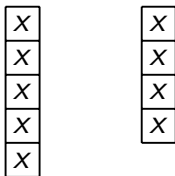
For example:



Why is it not enough to look just at the data?



Because of:



# Bidirectional Transformations

Some further relevant aspects:

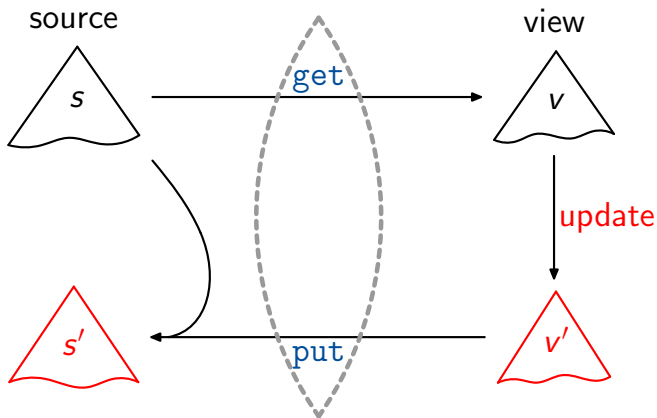
- ▶ What artifacts need to be specified?
  - ▶ both `get` and `put`
  - ▶ only one of them, the other derived
  - ▶ a more abstract artifact, from which both derivable
- ▶ How are they specified, manipulated, analyzed?
- ▶ What properties are they expected to have?
- ▶ What influence does a user, modeller, programmer have?

**Properties / Laws**



# Bidirectional Transformations

Specific asymmetric setting, state-based:

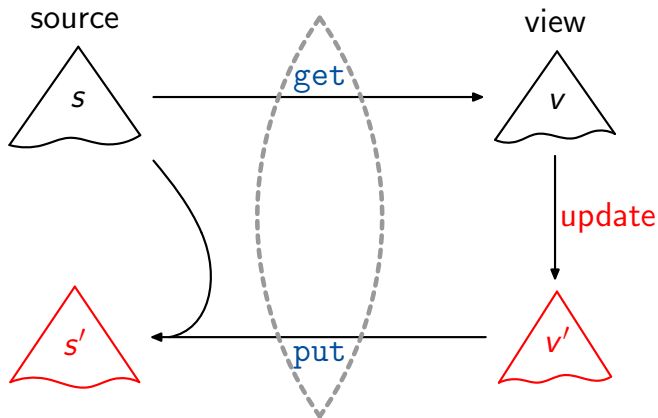


$get :: S \rightarrow V$

$put :: S \rightarrow V \rightarrow S$

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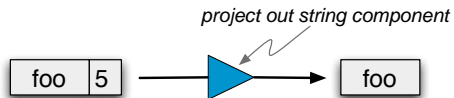


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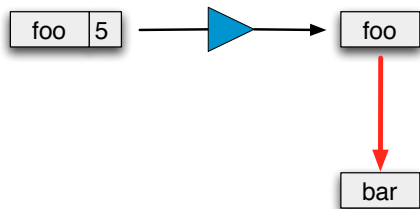
$put :: S \rightarrow V \rightarrow S$

assumed  
total!

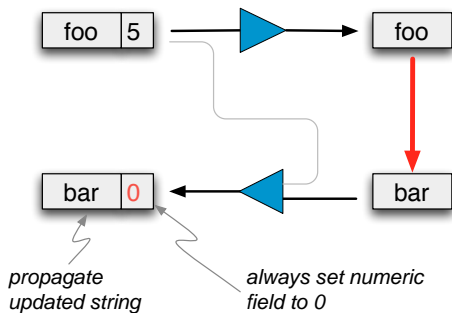
## About Behavior under No-Change



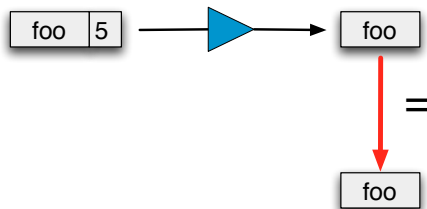
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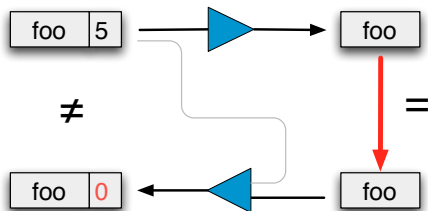
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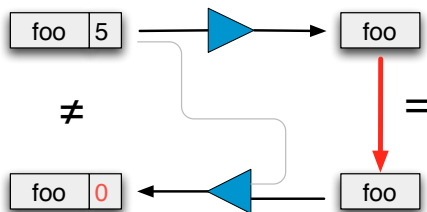
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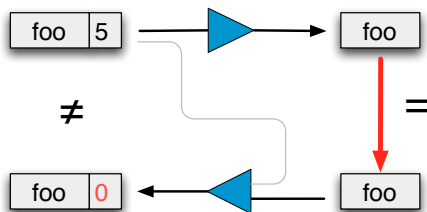
Principle: If the view does not change, neither should the source.

To prevent this, the GetPut law:

$$\text{put } s (\text{get } s) = s$$



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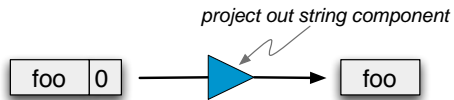
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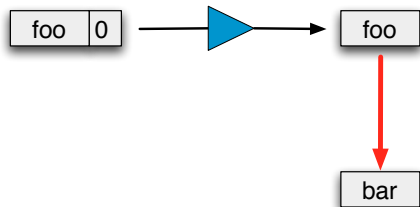
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NB: For this, `put` must be surjective.

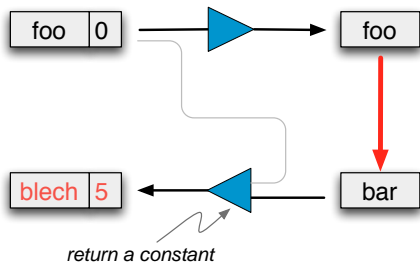
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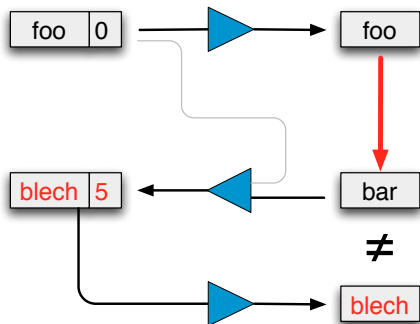
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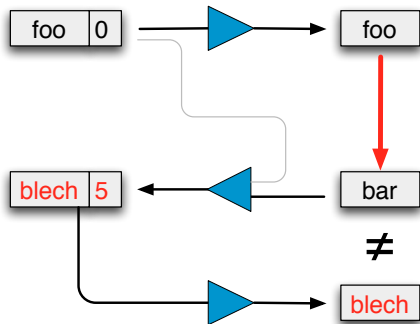
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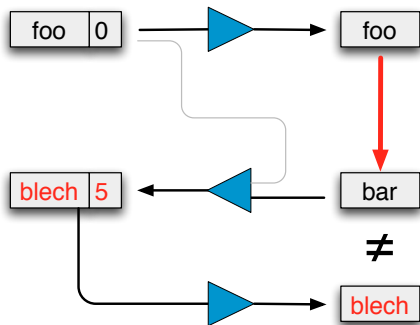


Principle: Updates should be translated exactly.

To prevent this, the PutGet law:

$$\text{get} (\text{put } s \ v) = v$$

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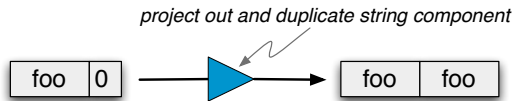
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NB: For this, `put s` must be injective for every `s`.

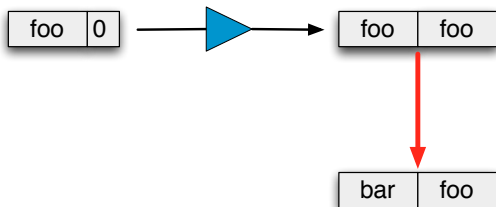
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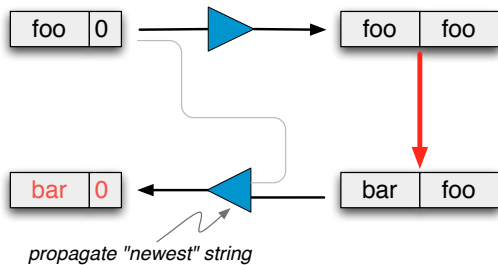




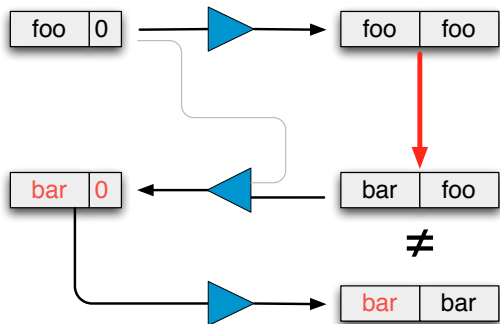
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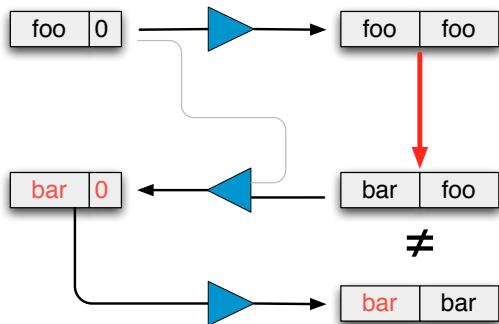
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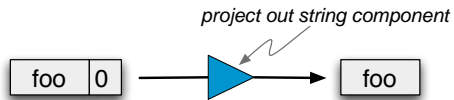


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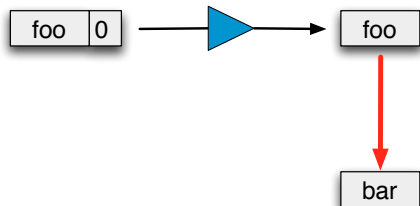


If we want to allow such behavior, we need to weaken the PutGet law (and people have done so).

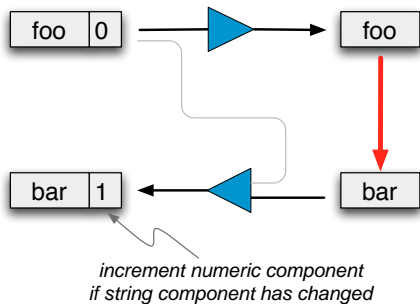
# About Consistent Composition



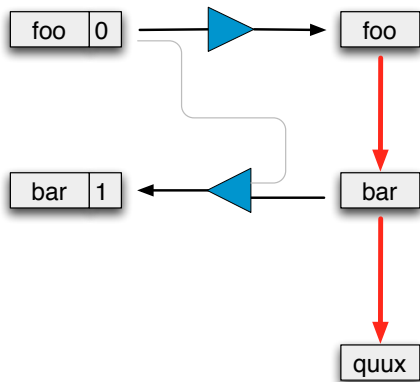
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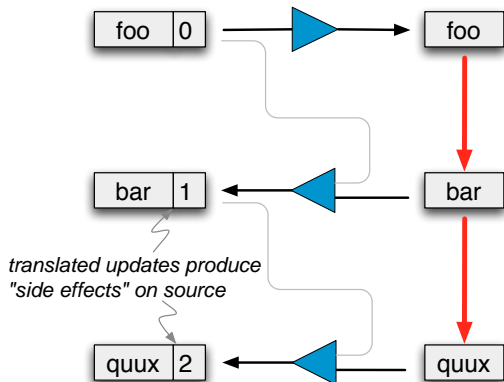


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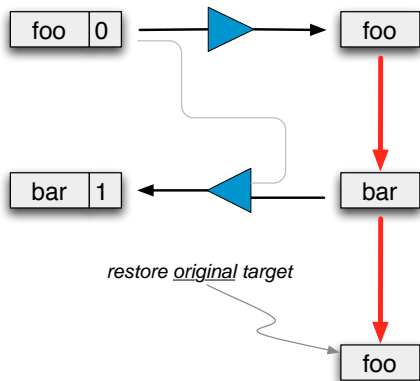




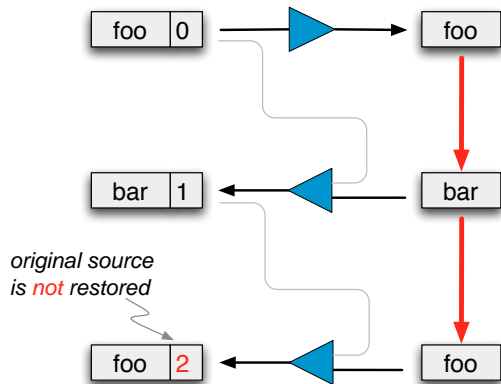
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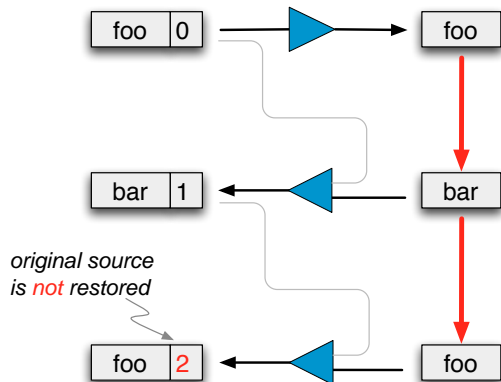
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## About Consistent Composition



To prevent this, the PutPut law:

$$\text{put } (\text{put } s \ v) \ v' = \text{put } s \ v'$$

## Less Debatable

Actually a consequence of GetPut and PutGet,  
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$$\text{put } (\text{put } s \ v) \ v = \text{put } s \ v$$

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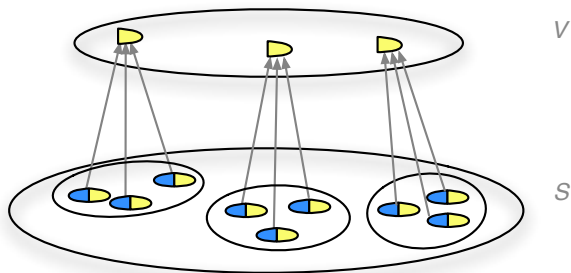
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We'll get back to this property in a moment.

**Ambiguity of put**

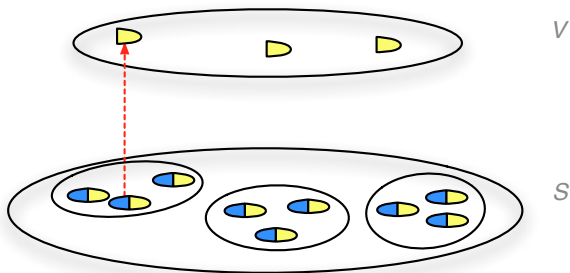
## How many puts are there?



Due to non-injectivity, `get` can map many objects from  $S$  onto the same object from  $V$ .

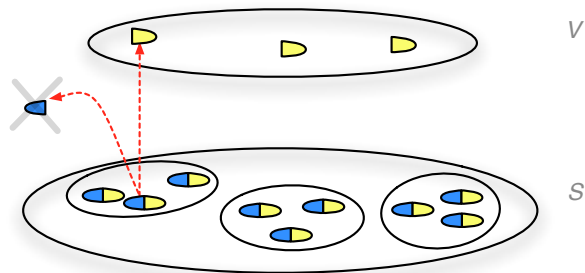


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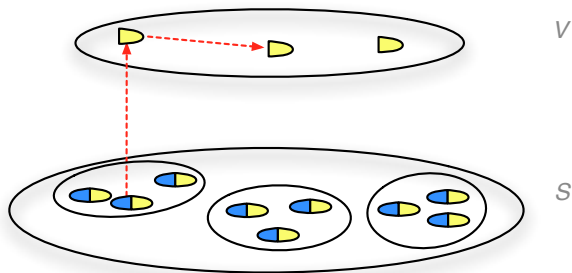
In essence, `get` projects out part of the information in the source object...

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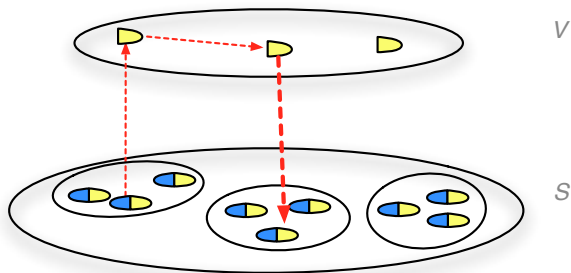
In essence, `get` projects out part of the information in the source object... and throws away the rest.

## How many puts are there?



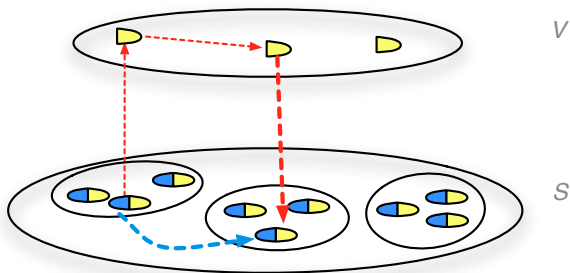
After an update,

## How many puts are there?



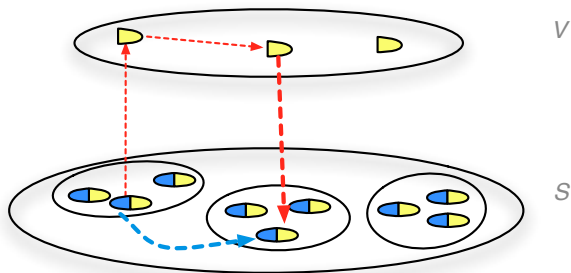
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## How many puts are there?



After an update, the “view part” of the new source object is fixed by PutGet. . . and if the lens obeys PutPut, the “projected away part” is fixed to be exactly the one from the original source.

## How many puts are there?

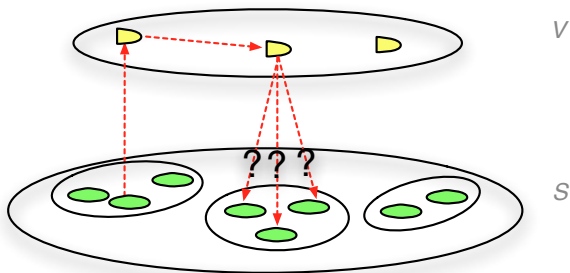


After a put, the “insertion” of the source  
object  
PutPut  
exactly the one from the original source.

Even this doesn't mean that there is  
only exactly one “very well-behaved”  
put per get!

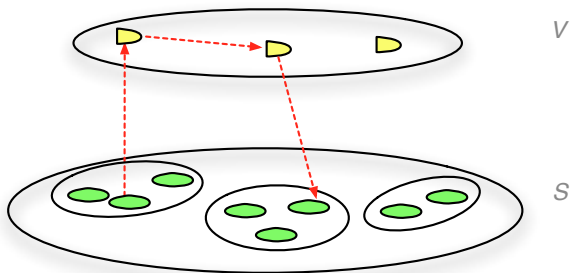
source  
obeys  
be

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Moreover, if the lens *doesn't* need to obey PutPut, then the behavior of `put` is much less constrained. . .  
. . . and there are even more `puts` to choose from!

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. . . and there are even more `puts` to choose from!

So, definitely need extra information to select one.



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... there is only one `get` per “well-behaving” `put`!

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[Fischer, Hu, Pacheco]

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... there is only one `get` per “well-behaving” `put`!

Specifically, if `put` is surjective, is injective for every  $s$ , and satisfies `PutTwice`, then there is *exactly* one `get` such that the two together satisfy `GetPut` and `PutGet`. And, there are equivalent, even nicer conditions formulated just in terms of `put` as well.

[Fischer, Hu, Pacheco]

There are even first concrete bidirectionalization techniques derived from this `put`-based approach!

**Conclusion / Discussion (?)**

## “Solved”

- ▶ a lot of very nice definitive work on semantics
- ▶ successful methods for automatic derivation of reasonable `put`- from `get`-functions on strings, trees, and graphs (?)
  - ▶ combinator languages with powerful type systems
  - ▶ program transformations based on constant-complement
  - ▶ query languages with automatic tracing
  - ▶ grammar-based approaches

## Open Problems

Leaving the academic niche:

- ▶ “How to deliver BX to the masses? Some effective way to integrate BX with existing general programming languages would be nice. Most tools/languages are very academic, and I don't see them being used for industrial case studies. . . .”
- ▶ “But I think to really achieve world domination, a BX framework will need to make substantial progress on having an attractive and intuitive front-end.”

## Open Problems

Tackling ambiguities effectively:

- ▶ “Can we design a declarative language that can be used to describe any intentional bidirectional behavior (i.e., have full control of bidirectional behavior)?”
- ▶ “We still lack effective, intuitive (user-friendly) and generic mechanisms to tame the non-determinism of backwards transformation.”
- ▶ “Ability to control the choice between multiple valid backward transformation results.  
[ . . . ] clarify to what extent user can control by writing different get (forward) transformations.”



## Open Problems

Handling richer semantic domains:

- ▶ “[. . .] still no effective solution for non-tree shaped domains.”
- ▶ “Bx on ordered graphs (outgoing edges are ordered) and graphs in which ordered and unordered edges are mixed.”
- ▶ “Handling of constraints over the domains (that is, handling non CFG-like domains). DB people have some work on this (handling keys, functional dependencies, inclusion dependencies, etc), but the issue seems ignored by PL people.”

## “Conclusion”

There is a lot of potential and possible inspiration from PL land for the general area of BX.

Challenges remain:

- ▶ scaling up in every way
- ▶ providing control over nondeterminism
- ▶ capturing user/programmer intentions
- ▶ handling richer structures/domains
- ▶ running efficiently